



# Forbush decrease model for expanding CMEs (ForbMod)

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**[mateja.dumbovic@uni-graz.at](mailto:mateja.dumbovic@uni-graz.at)**

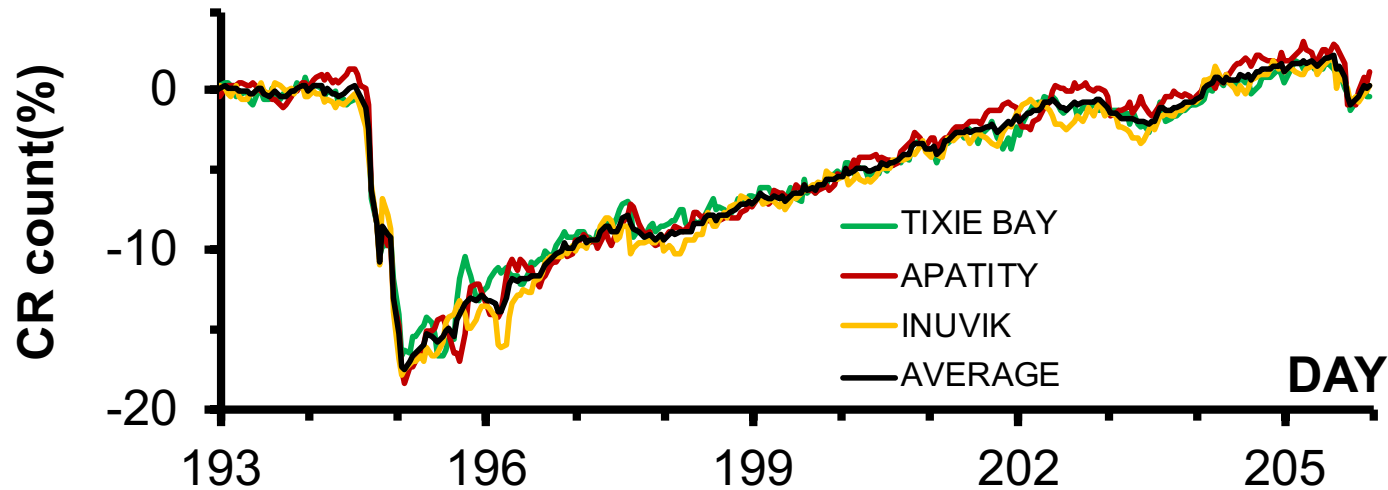
*1-Institute of Physics, University of Graz, Austria*

*2-Department of Extraterrestrial Physics, University of Kiel, Germany*

*3-Hvar Observatory, Faculty of Geodesy, University of Zagreb, Croatia*

*4-Karlovac University of Applied Sciences, Croatia*

# What are Forbush decreases?



*Dumbovic PhD thesis, 2015*

First observed by Forbush, 1937 and Hess & Demmelair, 1937

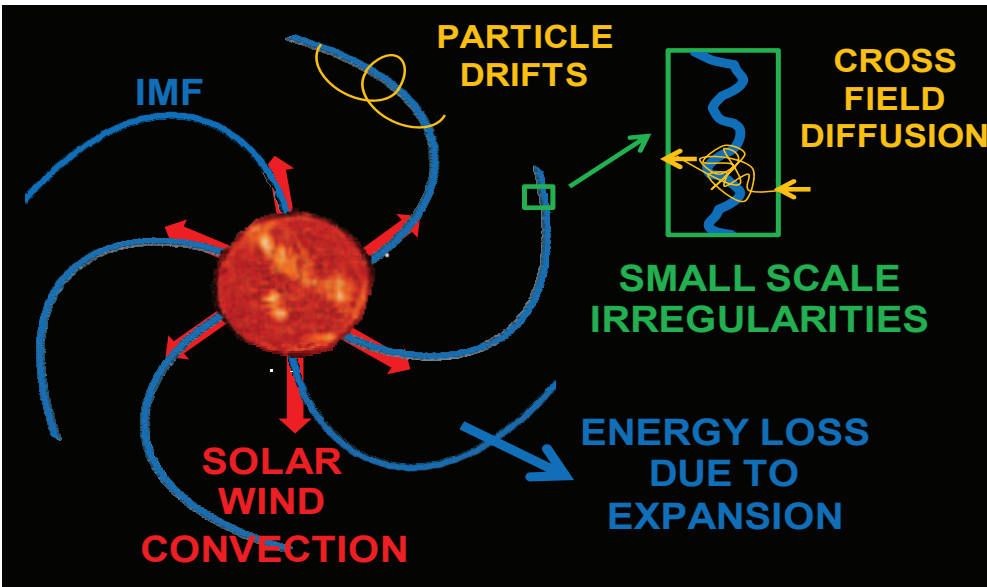
Short term decreases in galactic cosmic ray count

Typical duration several days

Typical amplitudes several %

(depends on the detector)

# Modulation of Galactic Cosmic Rays (GCRs) in Heliosphere



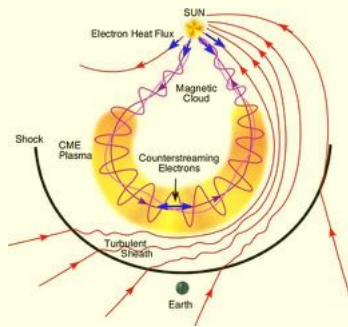
Dumbovic PhD thesis, 2015

PARTICLE TRANSPORT EQUATION  
Parker, 1965

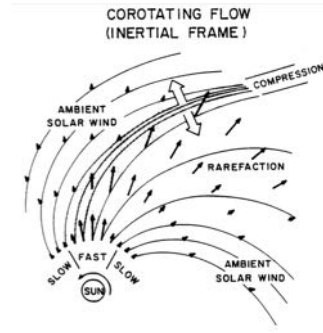
$$\underbrace{\frac{\partial f}{\partial t}}_a = -(\underbrace{\mathbf{V}}_b + \underbrace{\langle \mathbf{v}_d \rangle}_c) \cdot \nabla f + \underbrace{\nabla \cdot (\mathbf{K}_s \cdot \nabla f)}_d + \underbrace{\frac{1}{3} (\nabla \cdot \mathbf{V}) \frac{\partial f}{\partial \ln P}}_e$$

a → GCR phase-space distribution function  $F(P, t, r)$   
 b → convection  
 c → drifts  
 d → diffusion  
 e → Adiabatic cooling

# What causes Forbush decreases?

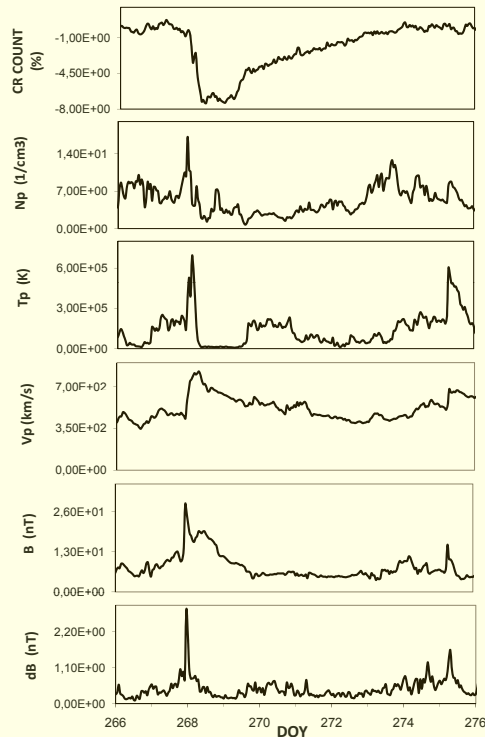


Zurbuchen&Richardson,2006

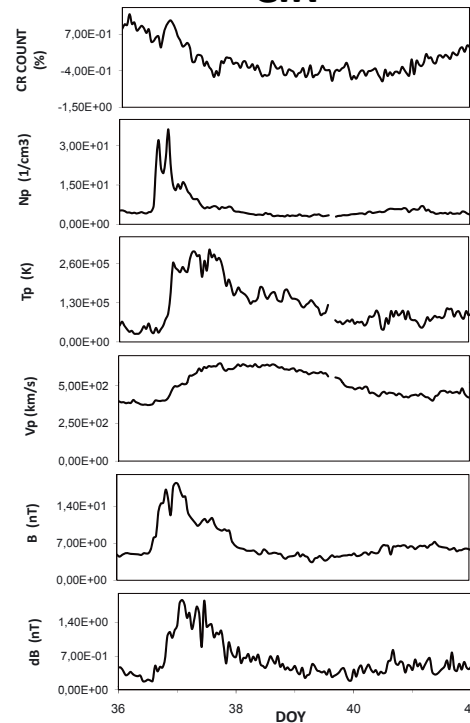


Gosling&Pizzo,1999

## ICME



## CIR



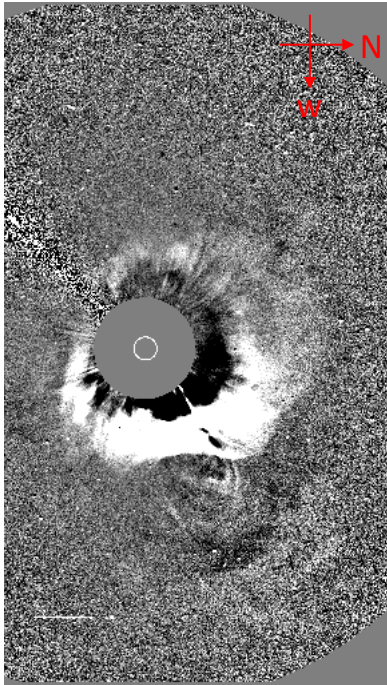
Various shapes and sizes



Various interplanetary transients

## Forbush decreases caused by Interplanetary Coronal Mass Ejections (ICMEs)

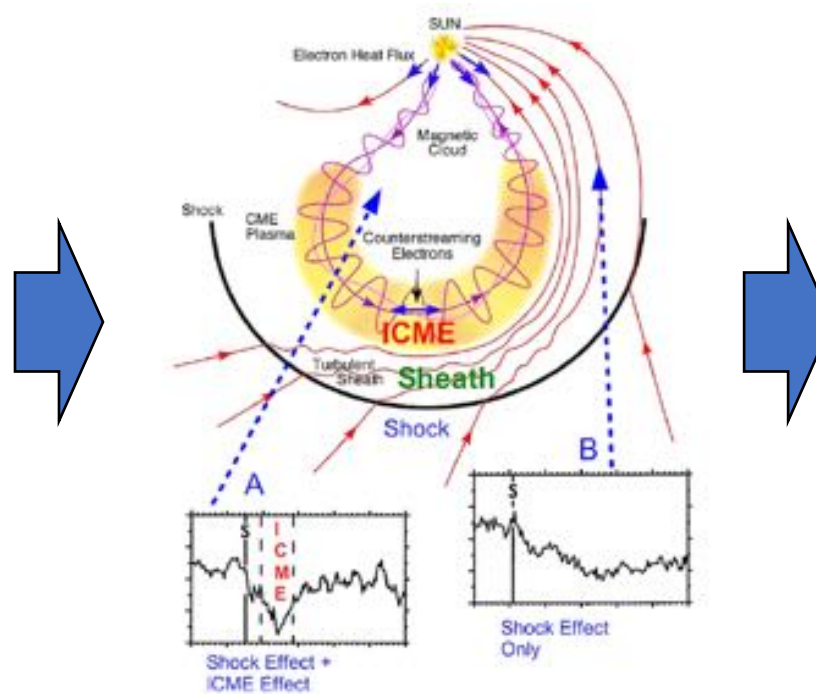
## REMOTE OBSERVATION



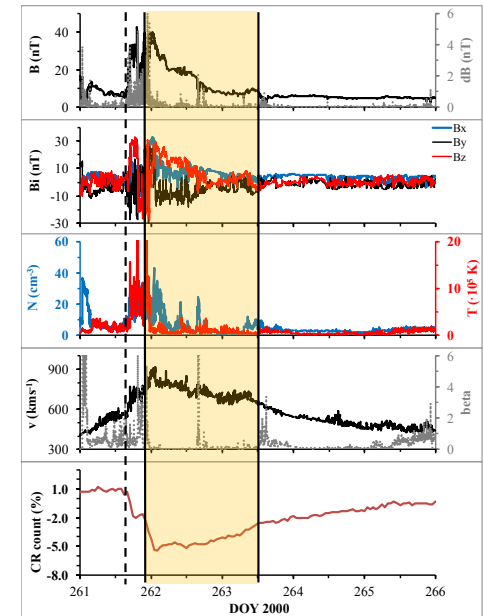
CME in SOHO/LASCO C3  
2000 September 16 06:18 UT  
First C2 detection at 05:18

## VISUALISATION

*Adapted from Richardson & Cane, 2011, SolPhys*



## IN SITU MEASUREMENTS

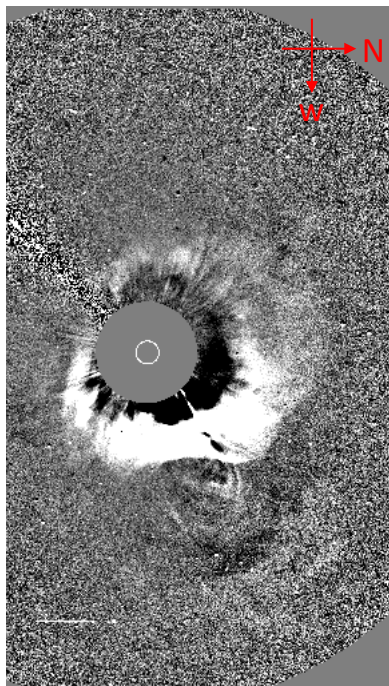


ICME detected in situ by Wind  
2000 September 17  
Shock arrival at 17:00

2step Forbush decrease detected by NMs at Earth  
*adapted from Dumbovic+, 2011, A&A*

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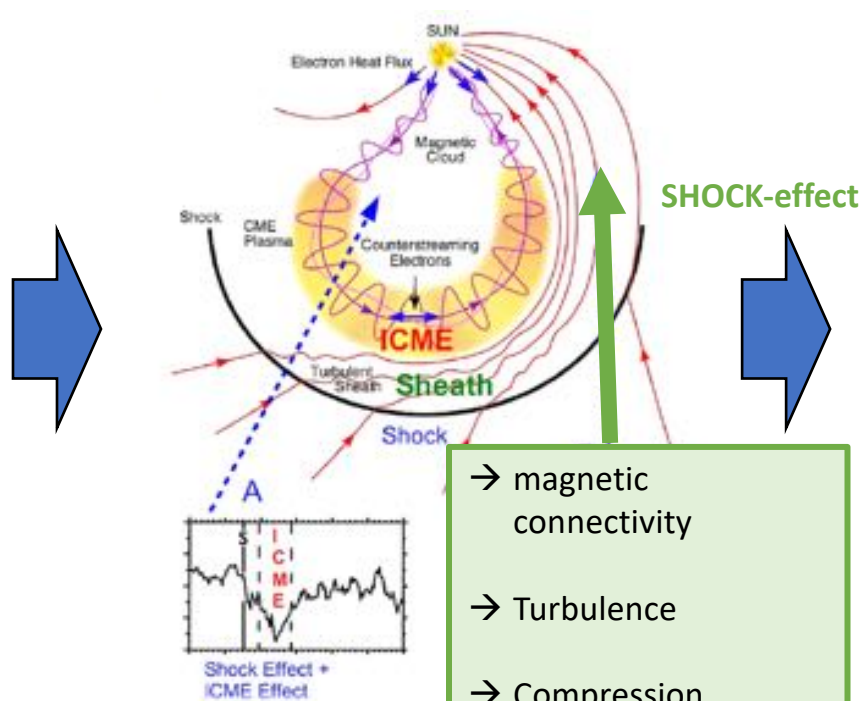
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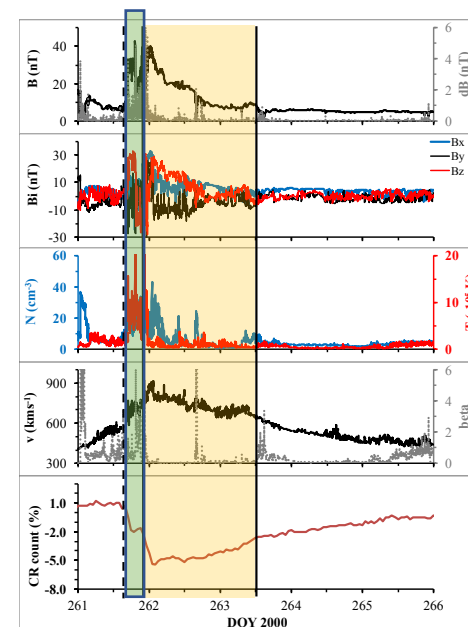
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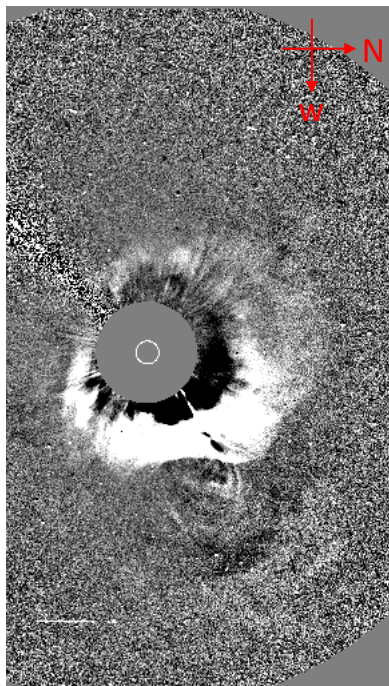
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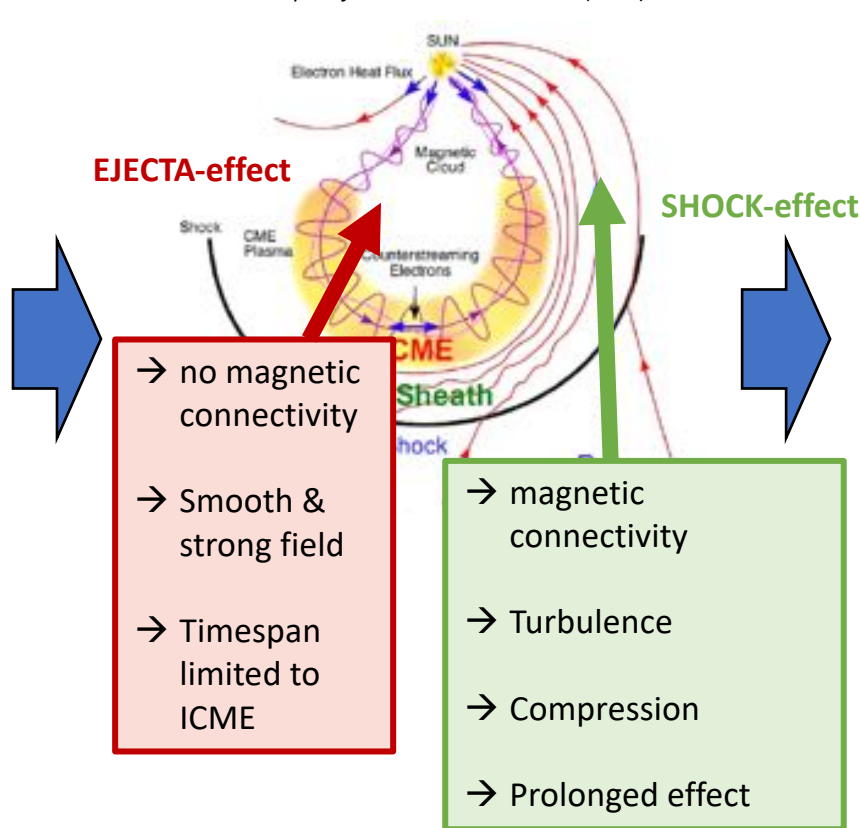
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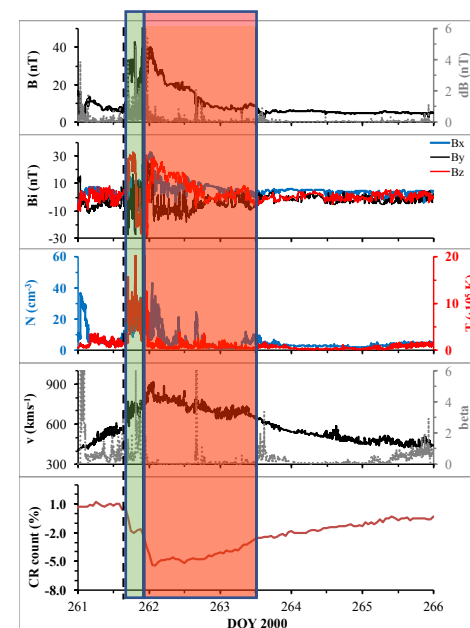
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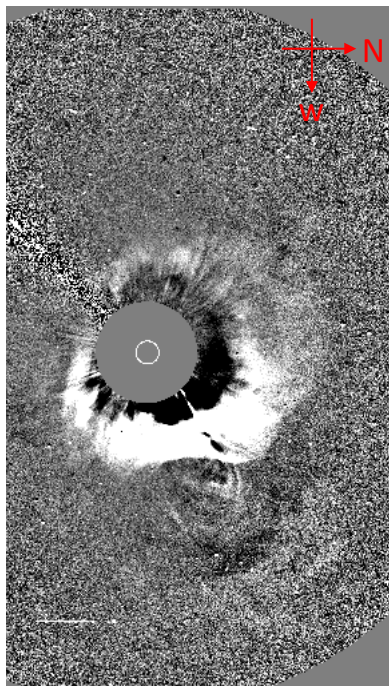


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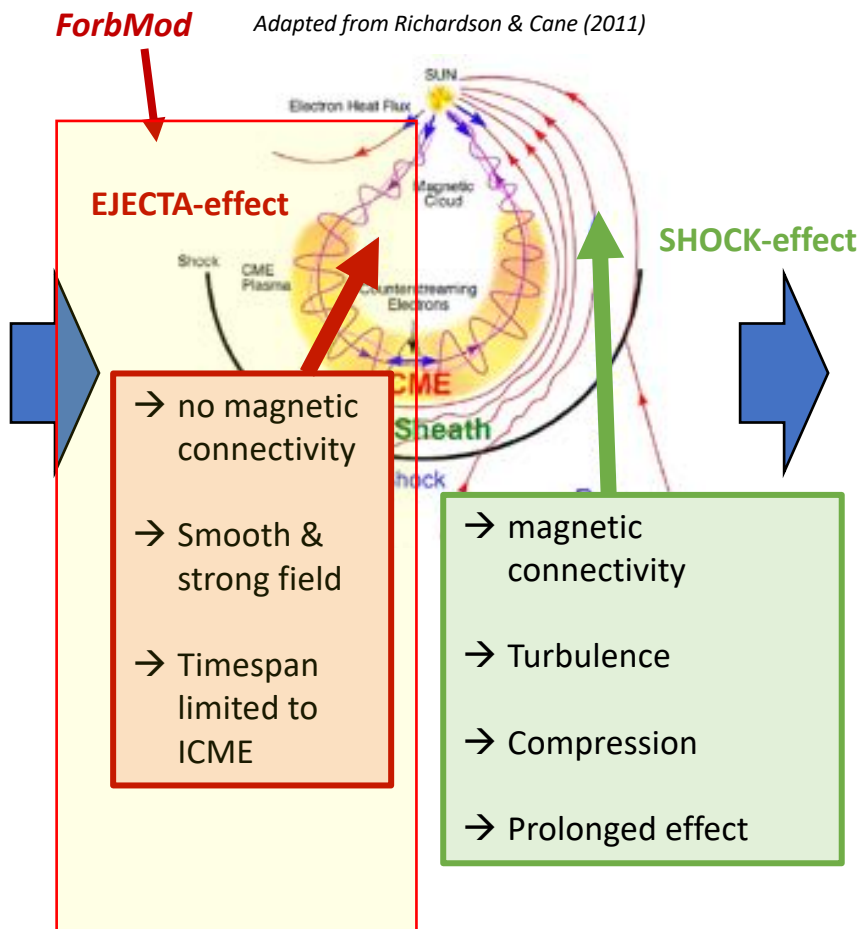
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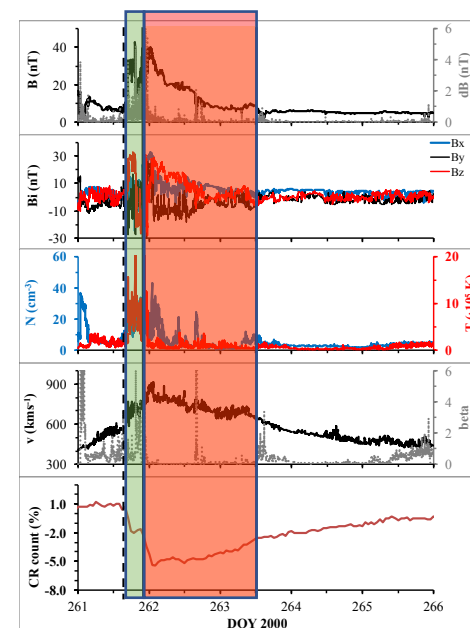
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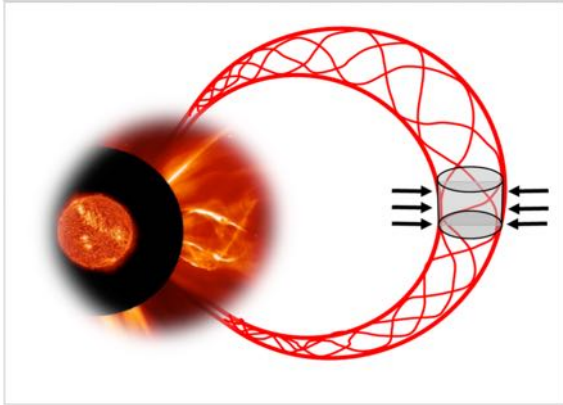
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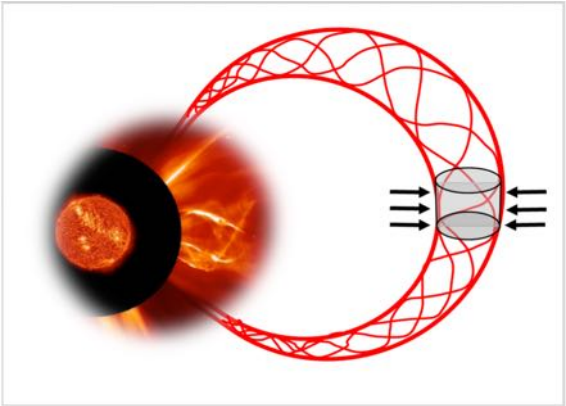
**ForbMod** = analytical diffusion-expansion model for Forbush decreases caused by flux ropes



- a closed magnetic structure
  - Initially empty of GCR
  - Locally of cylindrical form
- Moves with constant velocity

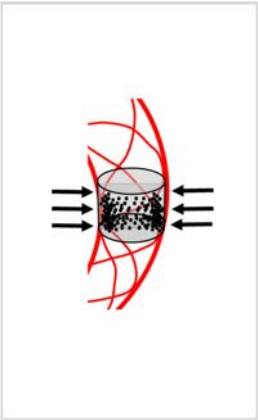
*First proposed by Morrison, 1956, PhysRev*

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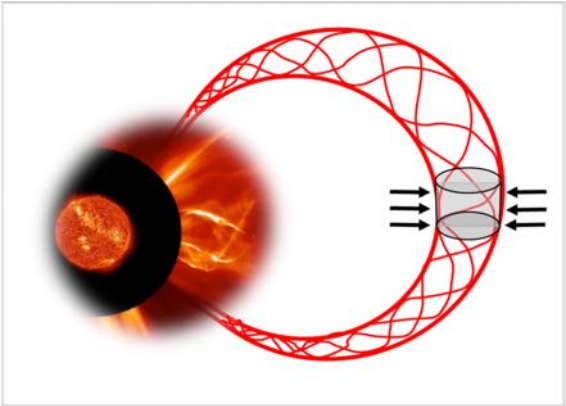
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- particles enter by perpendicular diffusion and slowly fill the structure

*Similar to e.g. Cane+, 1995, ICRCproc;  
Quenby+, 2008, JGR*

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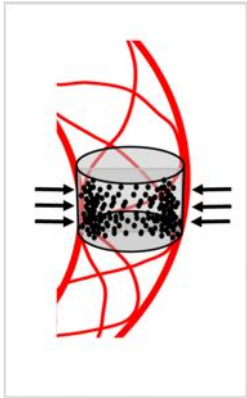
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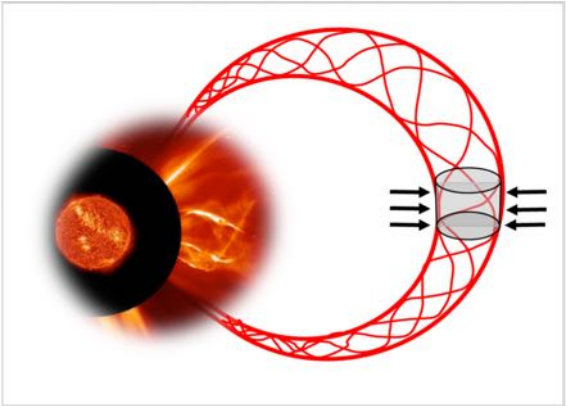
Similar to e.g. Cane+, 1995, ICRCproc;  
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- expands self-similarly

Similar to e.g. Munakata+, 2006, AdvGeophys;  
Arunbabu+, 2013, A&A

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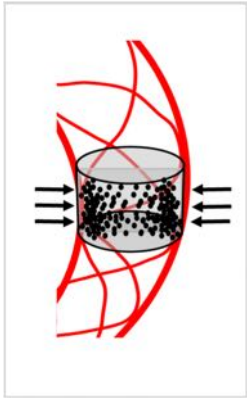
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$$U(r, t) = U_0 \left( 1 - J_0(\alpha_1 r) e^{-\alpha_1^2 f(t)} \right)$$

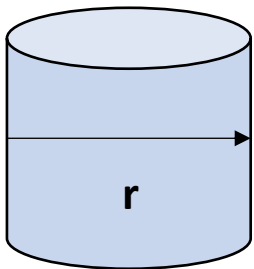
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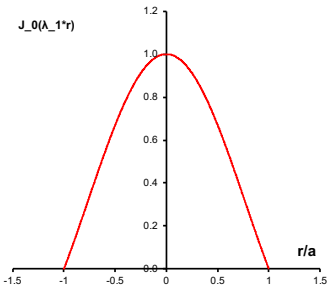
SPACE PART

TIME PART

Axial symmetry



Bessel function 0<sup>th</sup> order



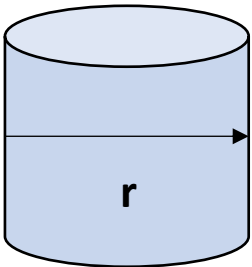
Symmetric + normalized

**ForbMod** = analytical diffusion-expansion model for Forbush decreases caused by flux ropes

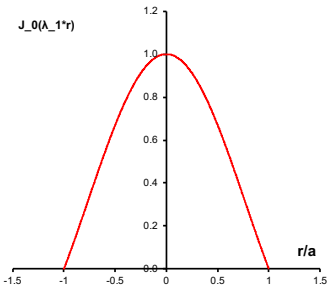
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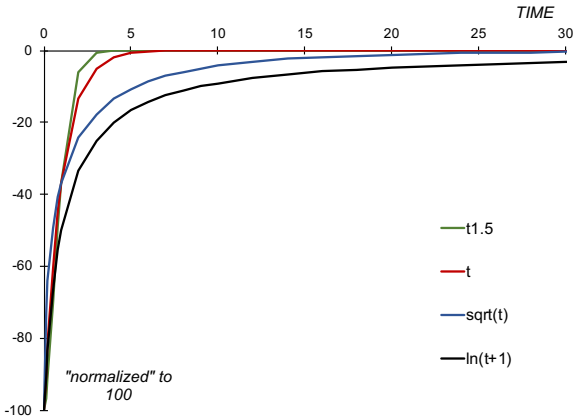


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Symmetric + normalized

TIME PART



Exponential function of time

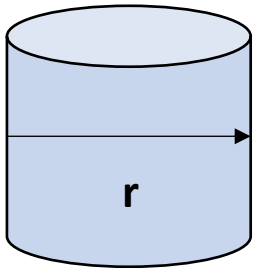
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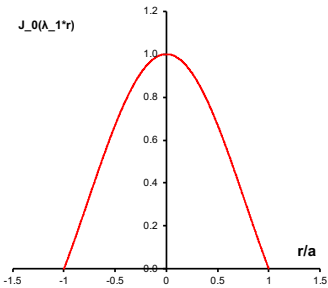
SPACE PART

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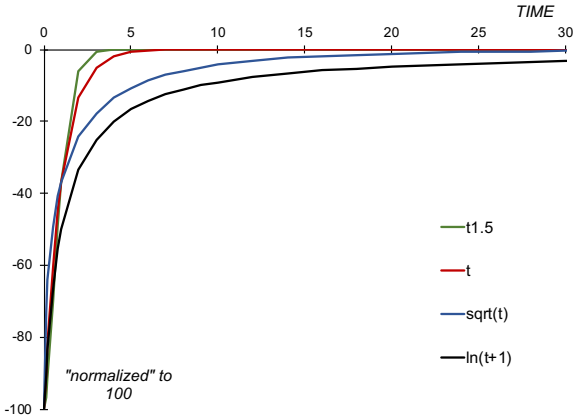
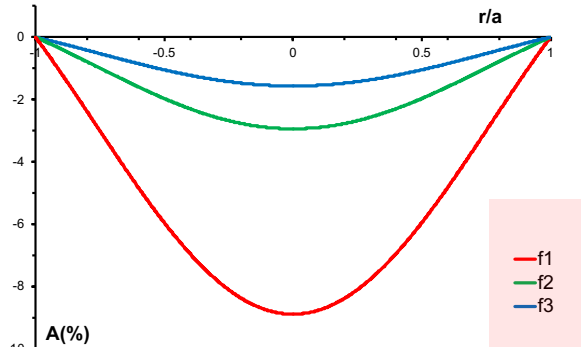
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Exponential function of time

**ForbMod** = analytical diffusion-expansion model for Forbush decreases caused by flux ropes

$$f(t) = \int D(t)/a(t)^2 dt$$

**ForbMod** = analytical diffusion-expansion model for Forbush decreases caused by flux ropes

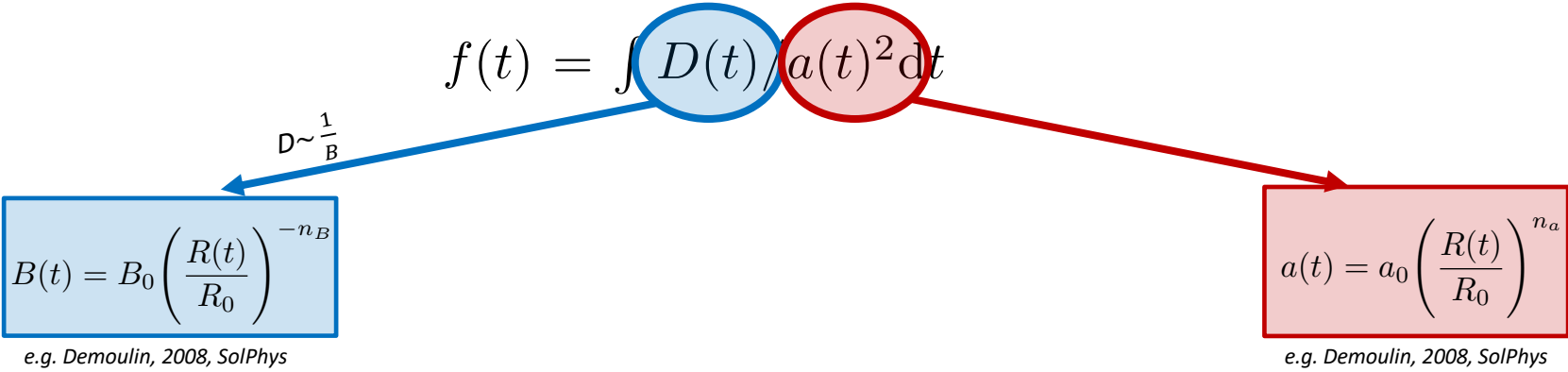
$$f(t) = \int D(t) / a(t)^2 dt$$

$D \sim \frac{1}{B}$

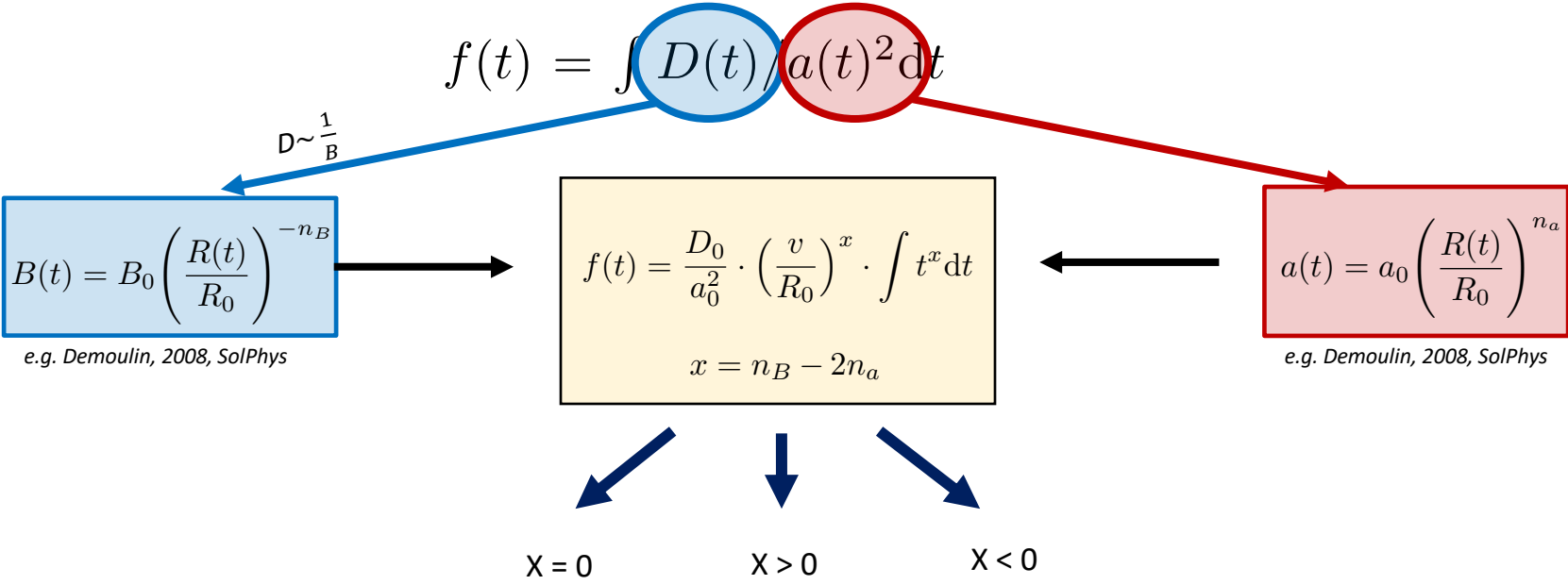
$$B(t) = B_0 \left( \frac{R(t)}{R_0} \right)^{-n_B}$$

e.g. Demoulin, 2008, SolPhys

**ForbMod** = analytical diffusion-expansion model for Forbush decreases caused by flux ropes



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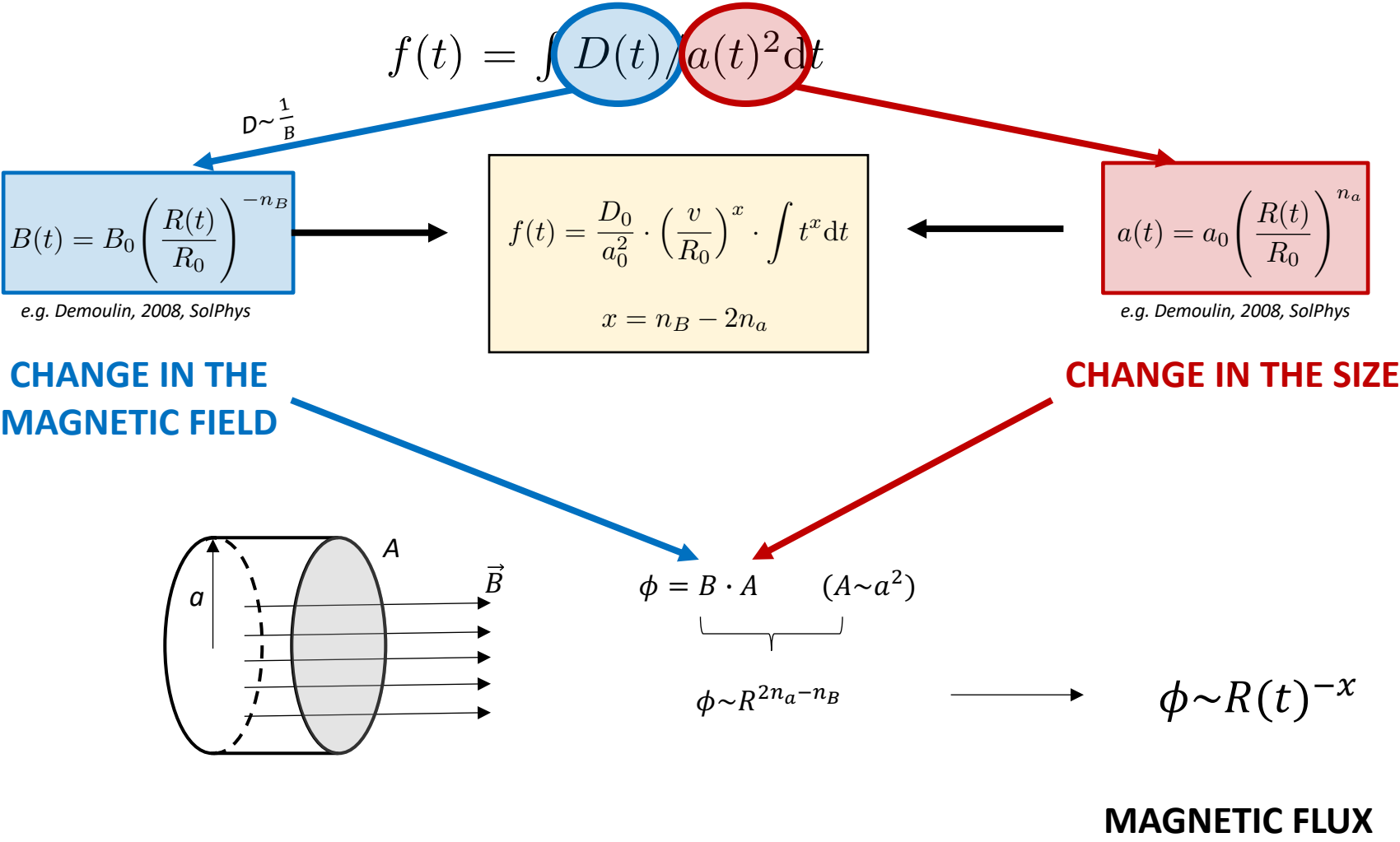


COMPETITION

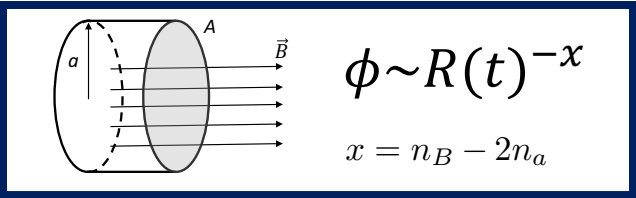
BETWEEN CHANGE IN THE MAGNETIC FIELD

AND THE CHANGE IN THE SIZE

**ForbMod** = analytical diffusion-expansion model for Forbush decreases caused by flux ropes

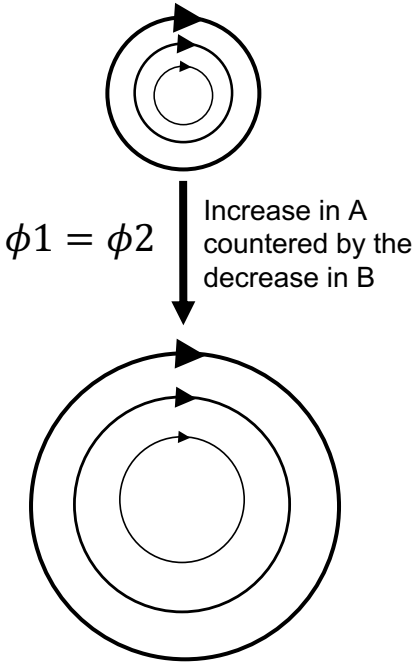


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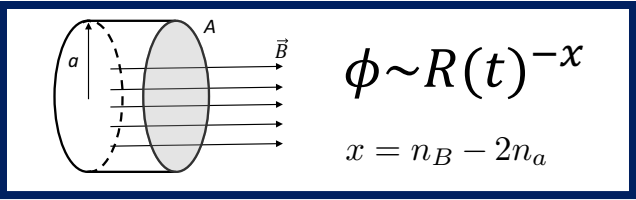


**MAGNETIC FLUX**

**X = 0**  
**(magnetic flux conserved)**



**ForbMod** = analytical diffusion-expansion model for Forbush decreases caused by flux ropes

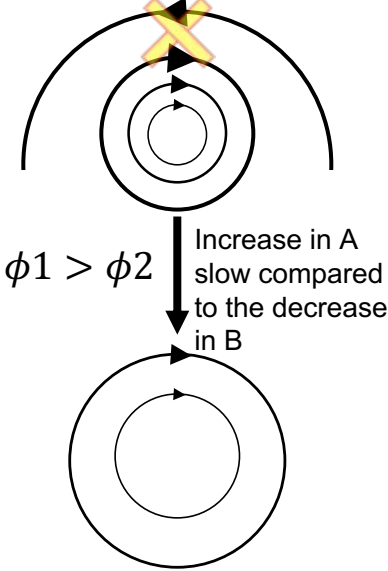
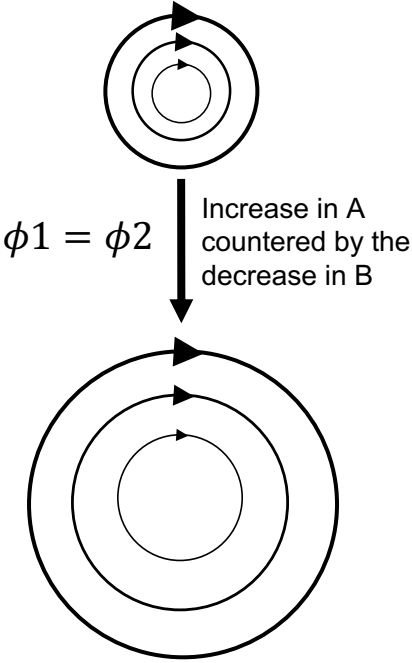


**MAGNETIC FLUX**

$$\phi \sim R(t)^{-x}$$
$$x = n_B - 2n_a$$

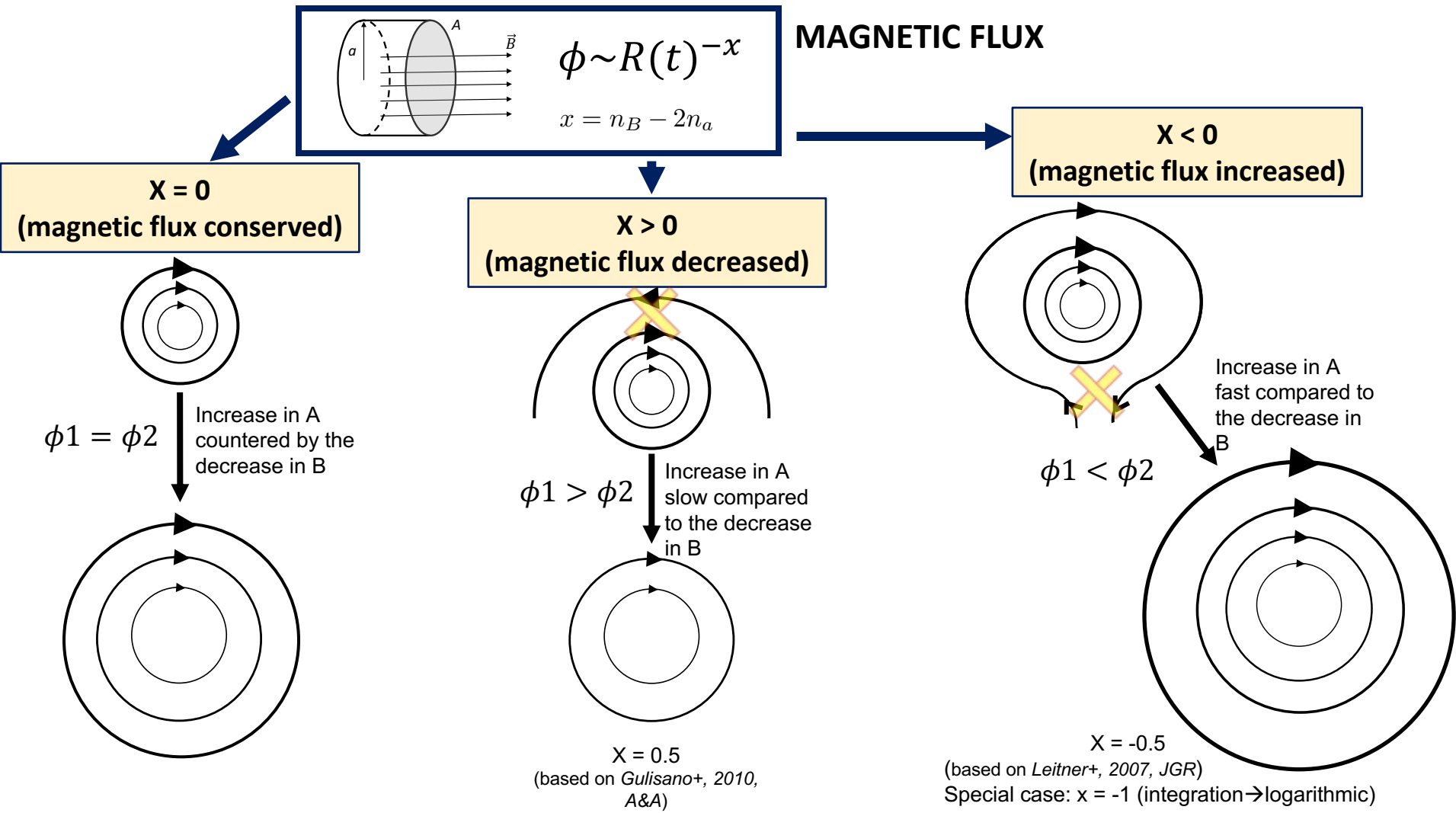
**X = 0**  
(magnetic flux conserved)

**X > 0**  
(magnetic flux decreased)

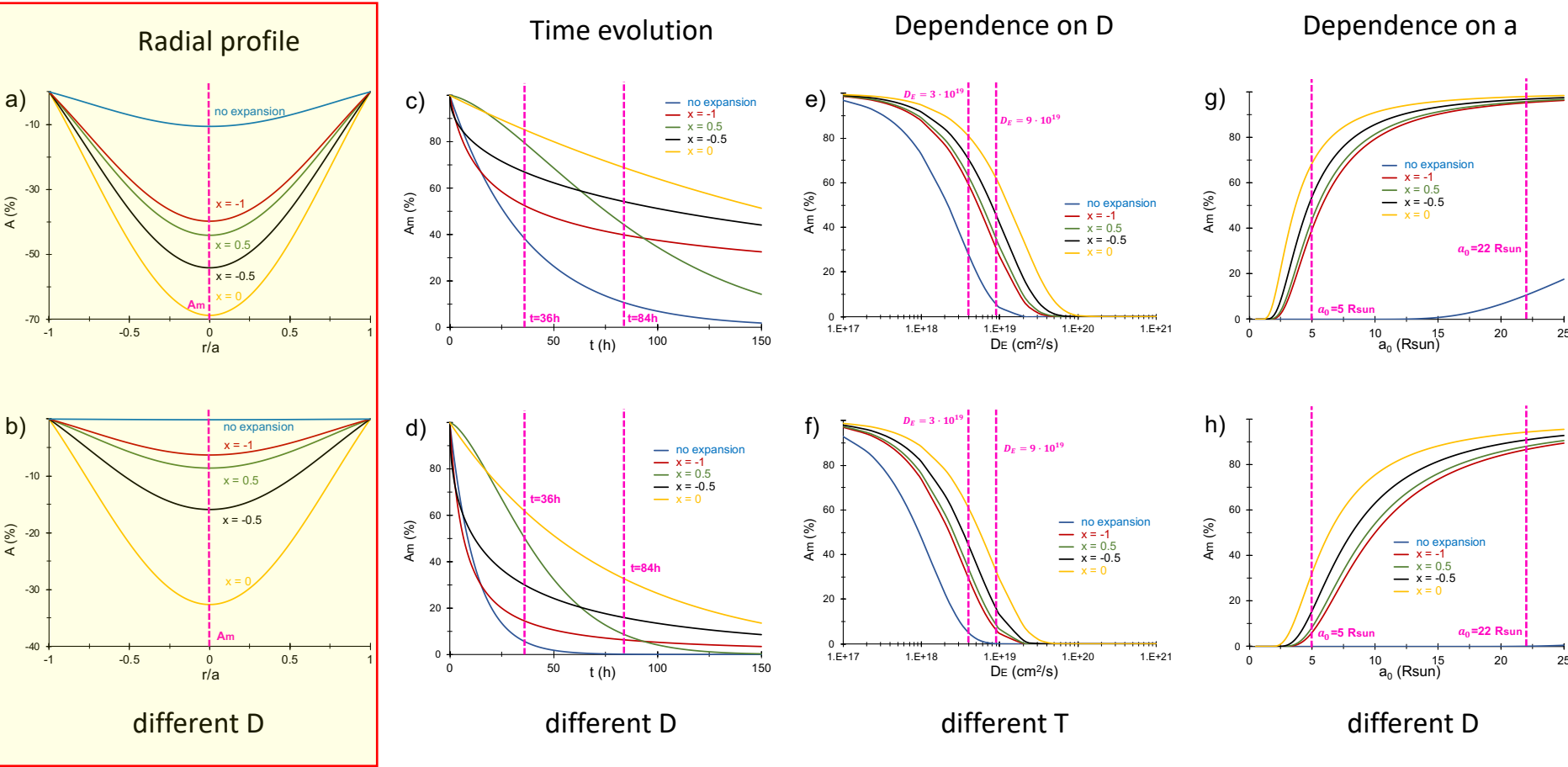


$X = 0.5$   
(based on Gulisano+, 2010, A&A)

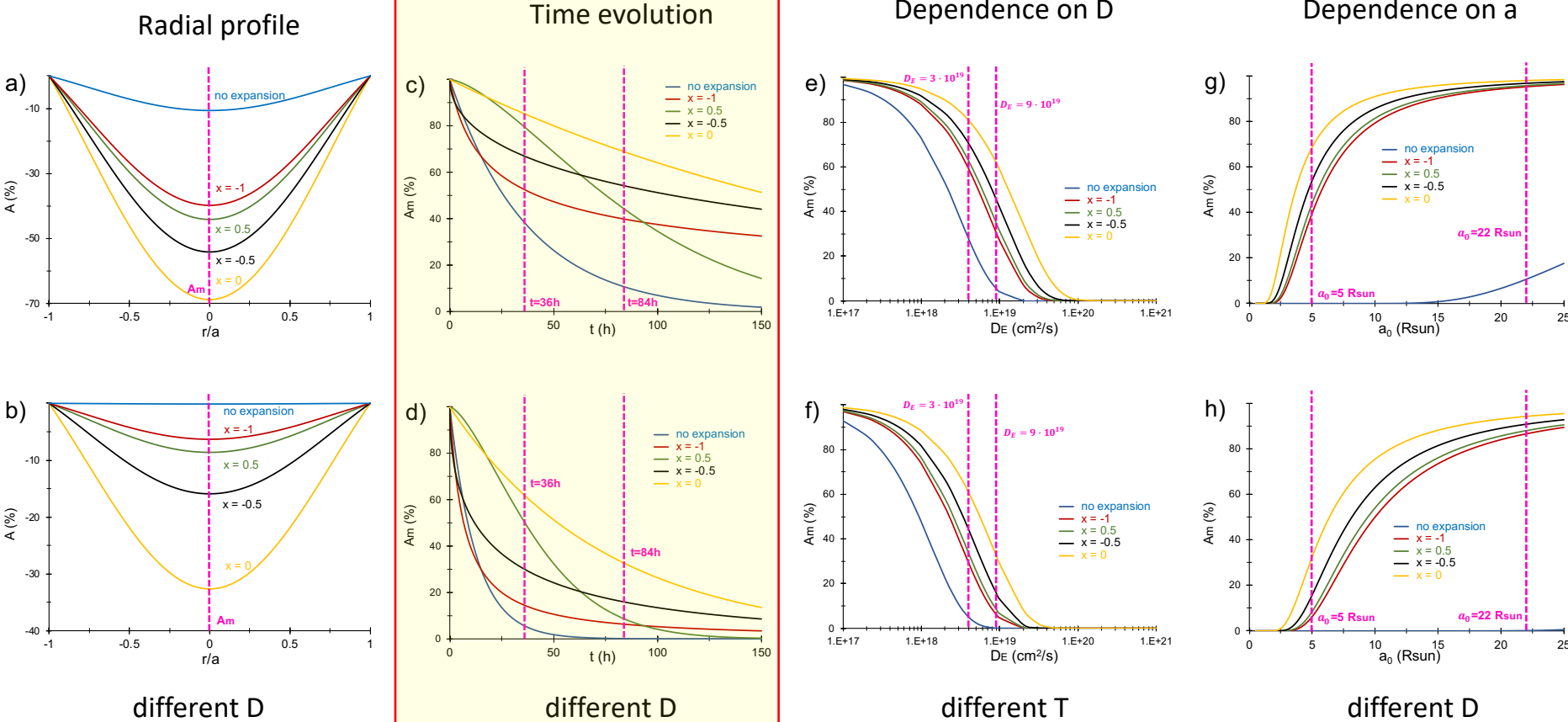
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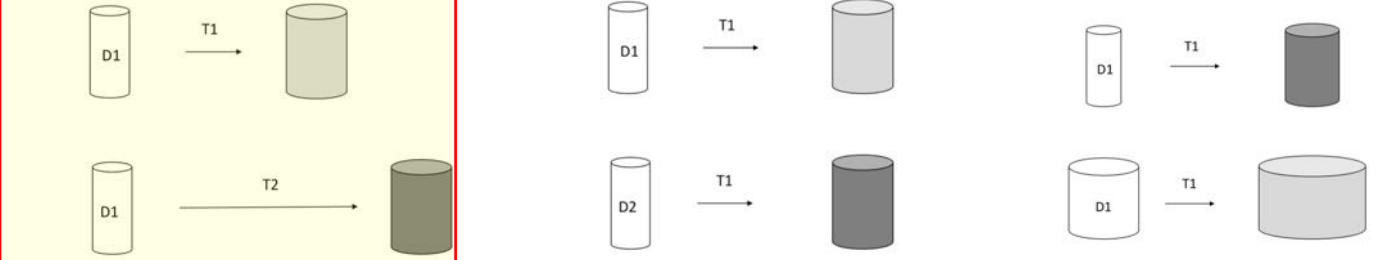
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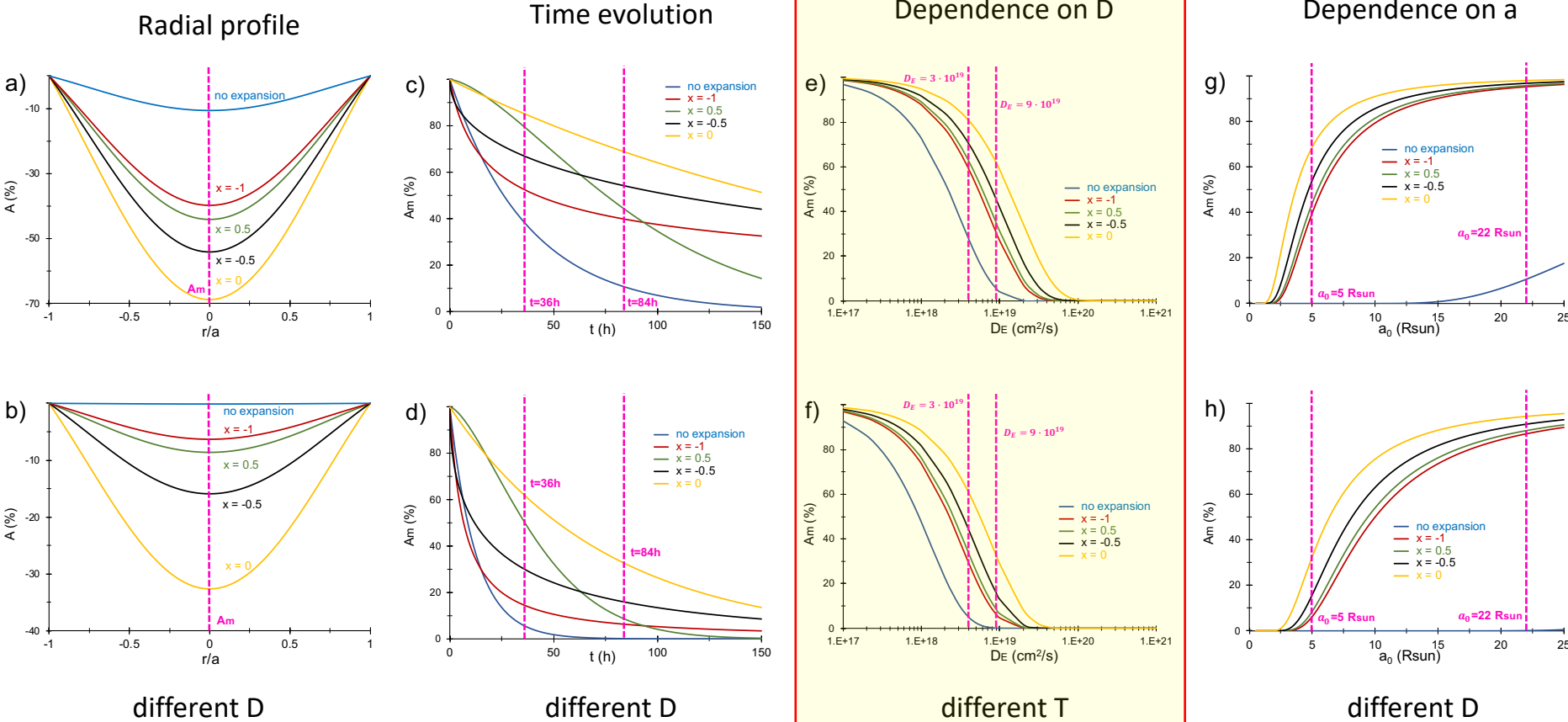
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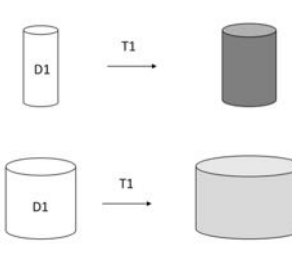
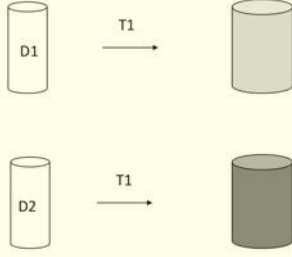
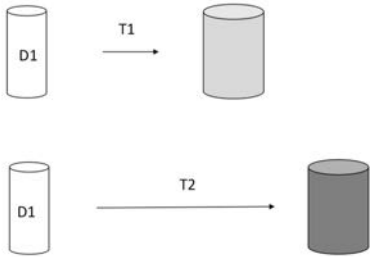
**COMPLEX  
INTERPLAY OF  
DIFFUSION AND  
EXPANSION**



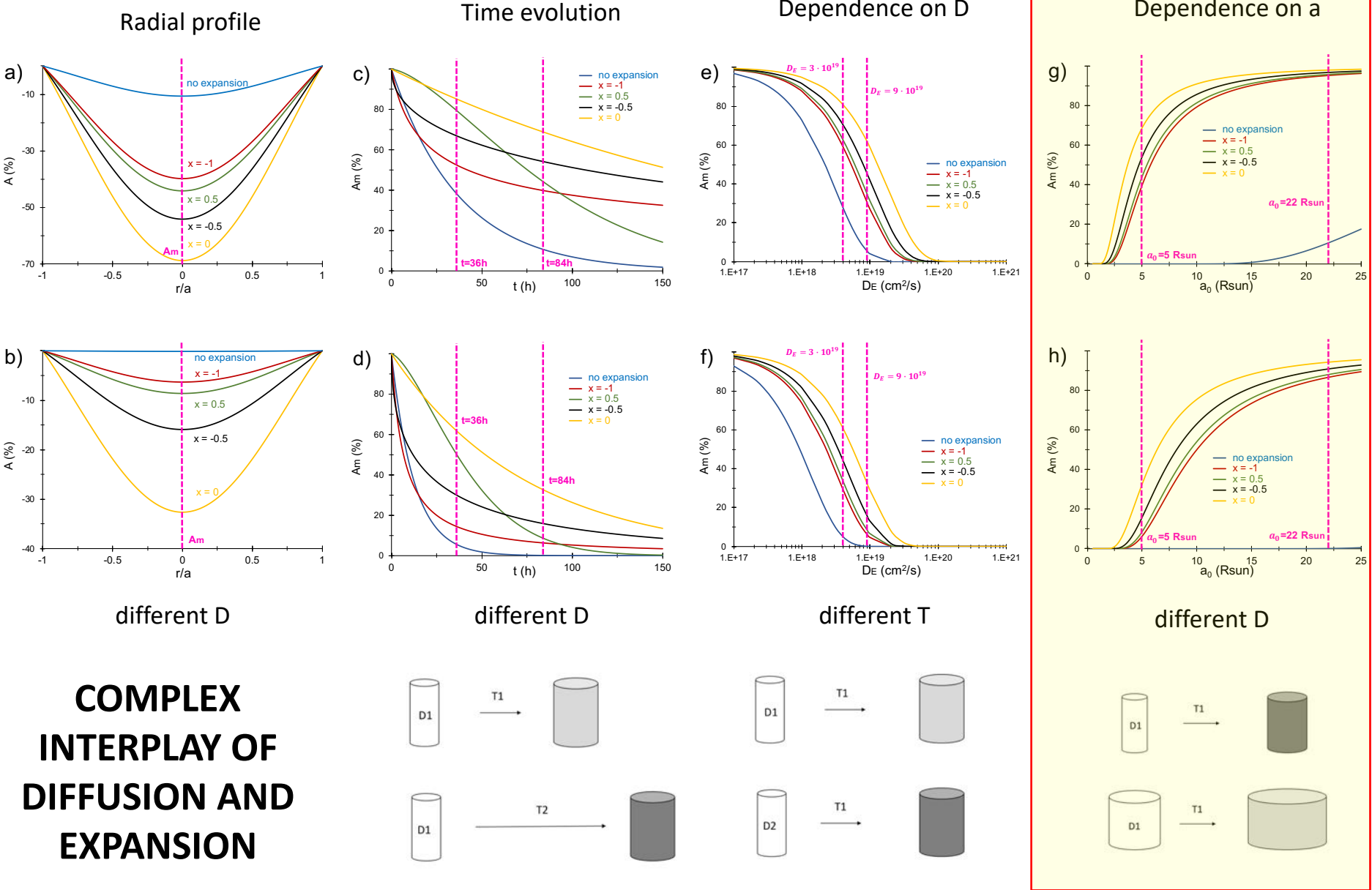
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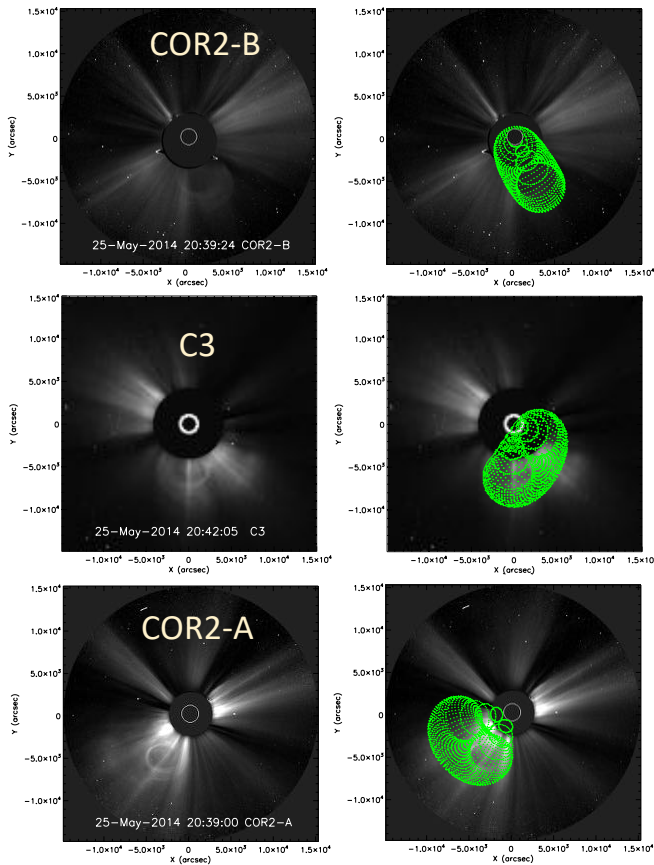
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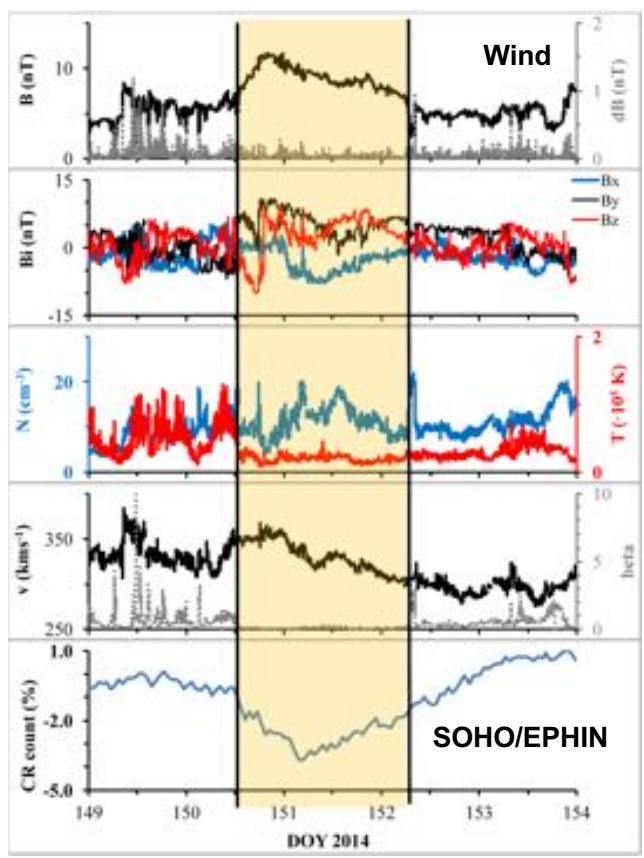
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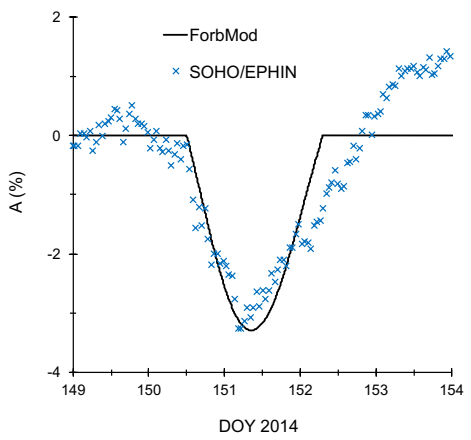
# THE CASE STUDY – TEST EVENT



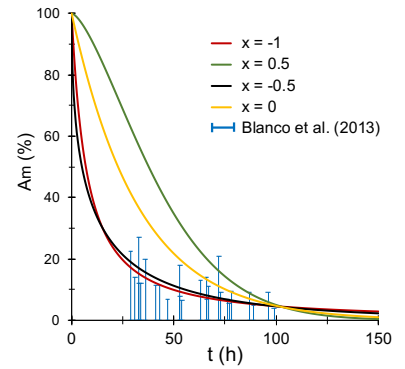
CME: 2014 May 25



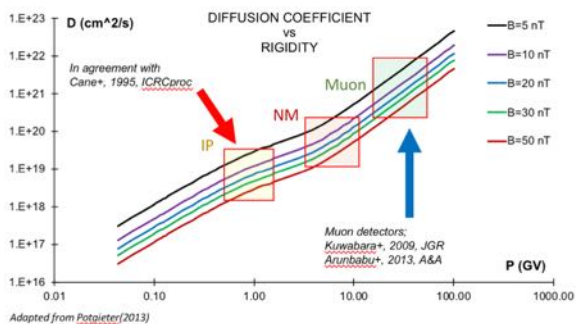
ICME & FD: 2014 May 30

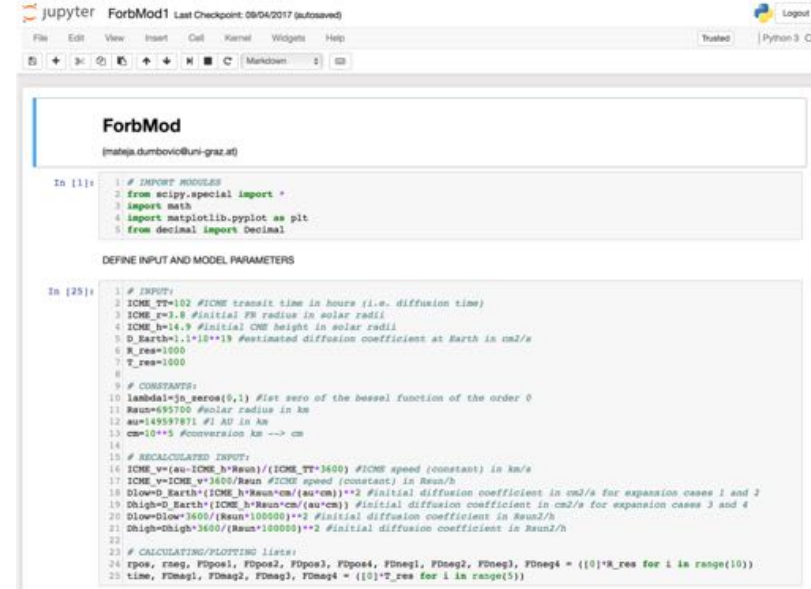


**BEST FIT**  
(diffusion coefficient free parameter)



**TIME EVOLUTION**  
model compared to observations from a statistical study by Blanco+, 2013  
(error bars = possible ejecta only FD range)





```
File Edit View Insert Cell Kernel Widgets Help Trusted Python 3 Q
In [11]: 1 # IMPORT MODULES
2 from scipy.special import *
3 import numpy
4 import matplotlib.pyplot as plt
5 from decimal import Decimal

DEFINE INPUT AND MODEL PARAMETERS

In [25]: 1 # INPUT:
2 ICME_TT=102 #ICME transit time in hours (i.e. diffusion time)
3 ICME_v=3.0 #initial FB radius in solar radii
4 ICME_h=14.9 #initial CME height in solar radii
5 D_Earth=1.1*10**19 #estimated diffusion coefficient at Earth in cm2/s
6 R_res=1000
7 T_res=1000
8
9 # CONSTANTS:
10 lambdal=jn_zeros(0,1) #1st zero of the bessel function of the order 0
11 R_sun=695700 #solar radius in km
12 au=149597871 # AU in km
13 cm=10**5 #conversion km --> cm
14
15 # RECALCULATED INPUTS:
16 ICME_v=(au-ICME_h*R_sun)/(ICME_TT*3600) #ICME speed (constant) in km/s
17 ICME_v=ICME_v*3600/R_sun #ICME speed (constant) in km/h
18 D_low=D_Earth*(ICME_h*R_sun*cm/(au*cm))**2 #initial diffusion coefficient in cm2/s for expansion cases 1 and 2
19 D_high=D_Earth*(ICME_h*R_sun*cm/(au*cm)) #initial diffusion coefficient in cm2/s for expansion cases 3 and 4
20 D_low=D_low*3600/(R_sun*100000)**2 #initial diffusion coefficient in km2/h
21 D_high=D_high*3600/(R_sun*100000)**2 #initial diffusion coefficient in km2/h
22
23 # CALCULATING/PLOTTING lists:
24 r_pos, r_neg, FD_pos1, FD_pos2, FD_pos3, FD_pos4, FD_neg1, FD_neg2, FD_neg3, FD_neg4 = ([0]*R_res for i in range(10))
25 time, FMag1, FMag2, FMag3, FMag4 = ([0]*T_res for i in range(5))
```

## CONCLUSIONS & FUTURE WORK

- *ForbMod* is analytical diffusion-expansion model for ejecta-only FDs
- FD amplitude depends on the interplay of diffusion and expansion
- Qualitatively agrees with observation
- Case study indicates quantitative agreement
- **NEXT STEPS:** testing and constraints using statistics, FR forward modeling and multispacecraft measurements

# Thank you for your attention!

Acknowledgements:



*The research leading to these results has received funding from the European Union's Horizon 2020 research and innovation programme under the Marie Skłodowska-Curie grant agreement No 745782.*